



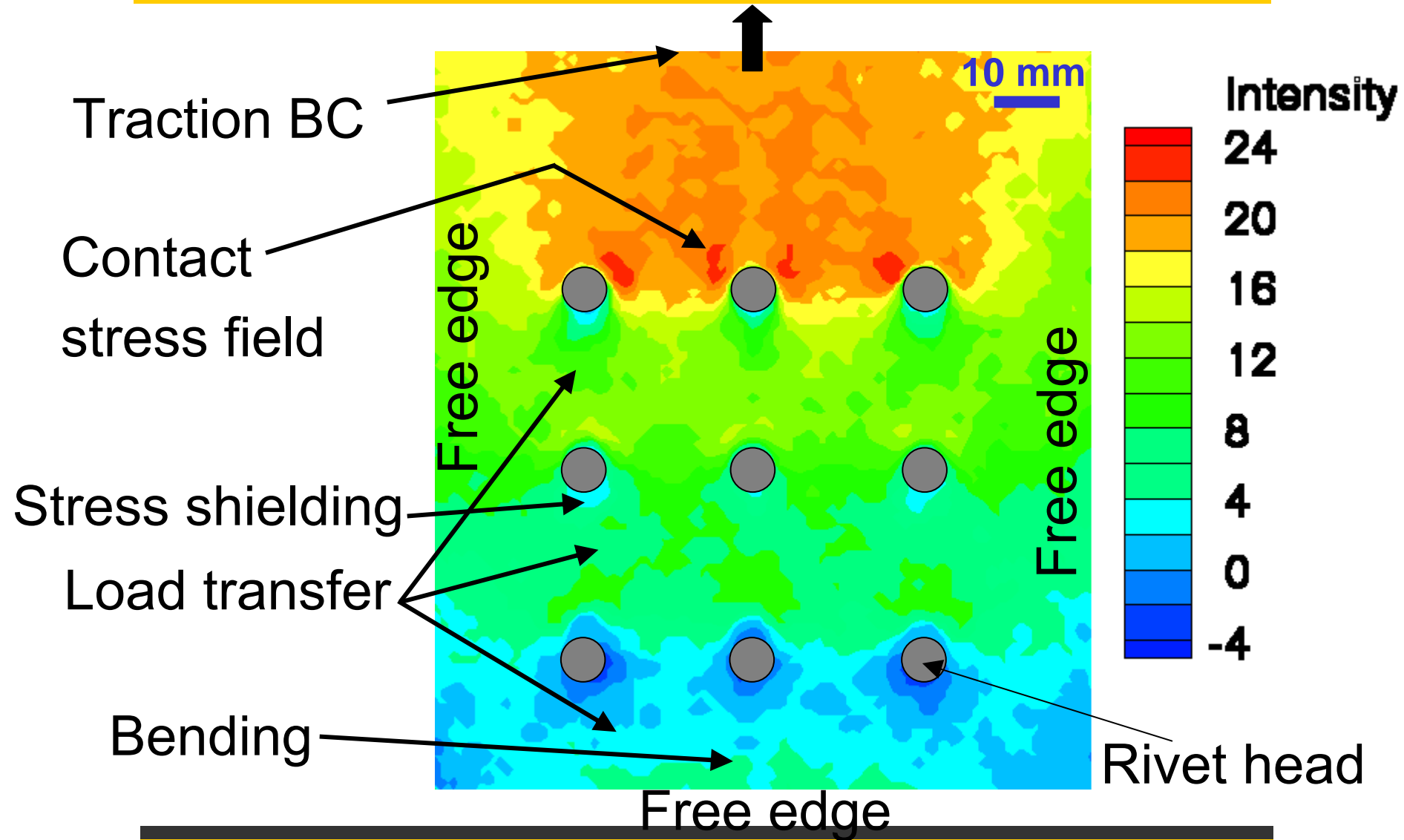
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# Recent Developments for Conformal Contacts with Friction

**N Sundaram  
TN Farris  
Purdue University**



# Applications ( $\sigma_o = 110$ MPa)

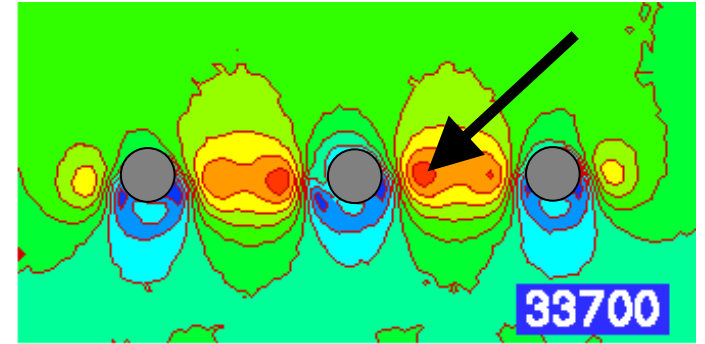
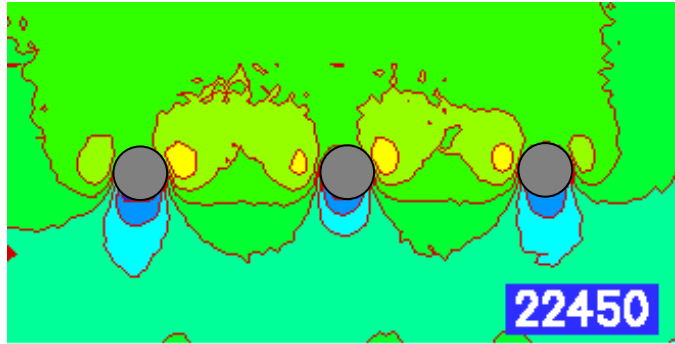




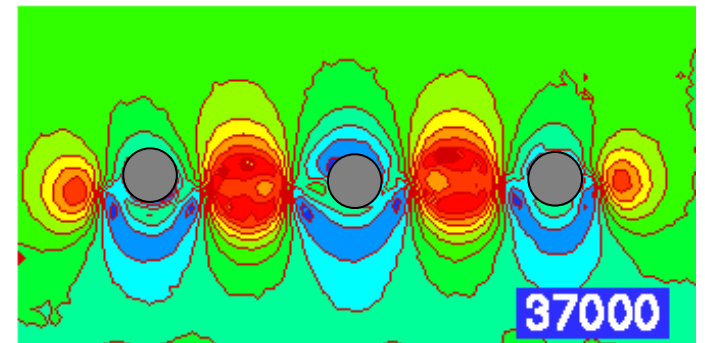
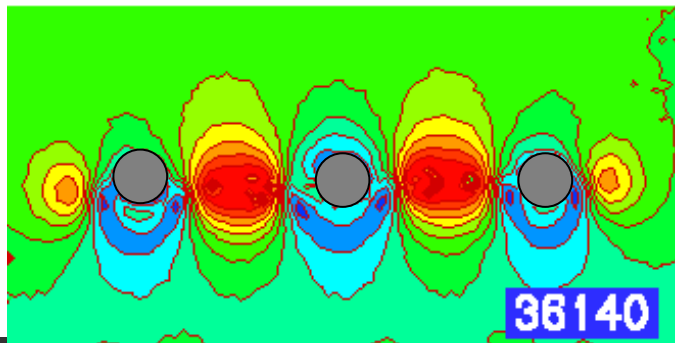
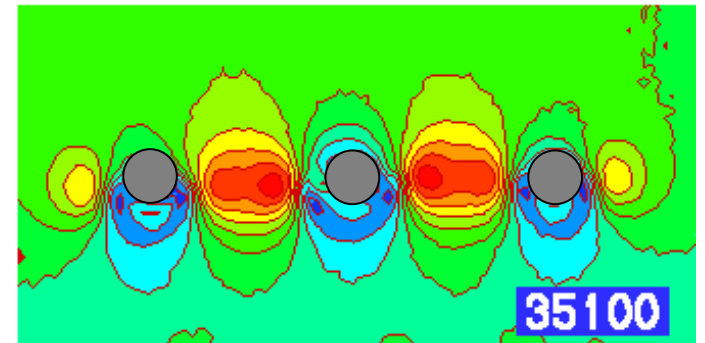
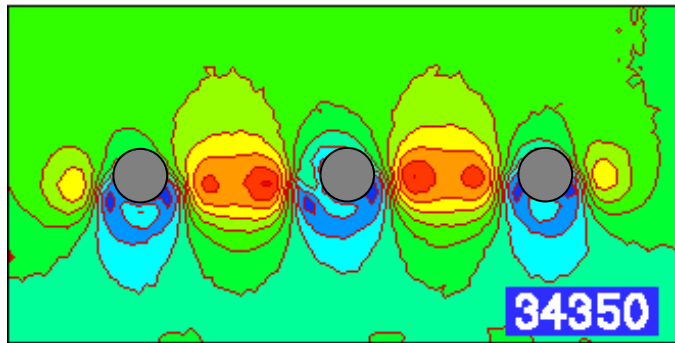
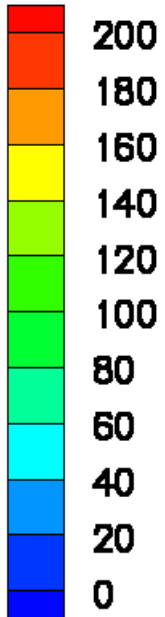
# Crack Evolution

$\sigma_o = 110$  MPa

cycles to failure = 37500



Eqv.  $\Delta\sigma_{kk}$  (Mpa)





# Rigid-on-iso, Full Sliding

- Full sliding SIDE obtained from the coupled system derived earlier  
Solution scheme: Transform Hilbert kernel to Cauchy kernel, solve with Gauss-Chebyshev quadrature and Newton-Raphson search.
- Full sliding solution is interpreted as being caused by applied CW / CCW moments under the prevailing P,Q, remote stress conditions
- The moments inducing sliding are obtained as part of the solution

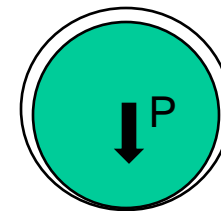
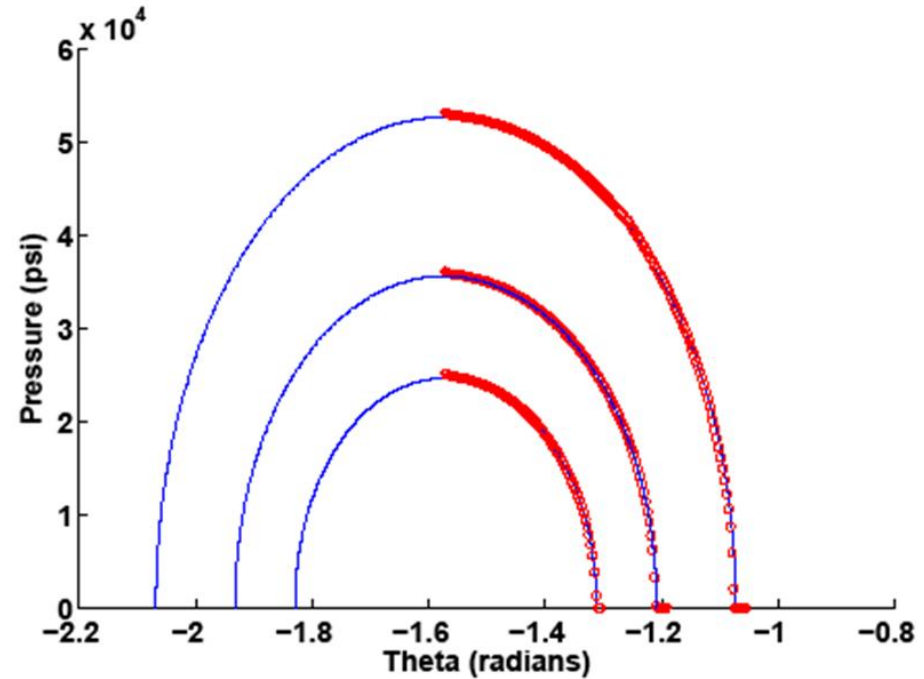
$$k'' = \kappa - 1 \quad k' = \frac{\kappa+1}{2} \quad \mathcal{A} = \sigma_{xx}^{\infty} + \sigma_{yy}^{\infty} \quad \mathcal{D} = \sigma_{xx}^{\infty} - \sigma_{yy}^{\infty}$$

$$\begin{aligned} -R + R_D - \frac{Rk'}{2G} \left[ \frac{A}{2} - 3D \cos(2\theta) \right] &= \frac{R}{4\pi G} \left[ k' \int_{\alpha}^{\beta} N(\xi) d\xi + 2\kappa \int_{\alpha}^{\beta} \cos(\theta - \xi) N(\xi) d\xi \right. \\ &\quad \left. - k' \int_{\alpha}^{\beta} \cot \left( \frac{\theta - \xi}{2} \right) N'(\xi) d\xi - \pi k'' N(\theta) \pm \mu k' \int_{\alpha}^{\beta} \cot \left( \frac{\theta - \xi}{2} \right) N(\xi) d\xi \right. \\ &\quad \left. \mp \mu 2\kappa \int_{\alpha}^{\beta} \sin(\theta - \xi) N(\xi) d\xi \mp \pi k'' \mu N'(\theta) \quad \forall \theta \in (\alpha, \beta) \right] \end{aligned}$$



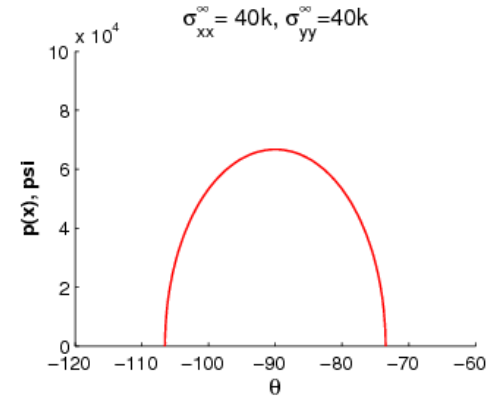
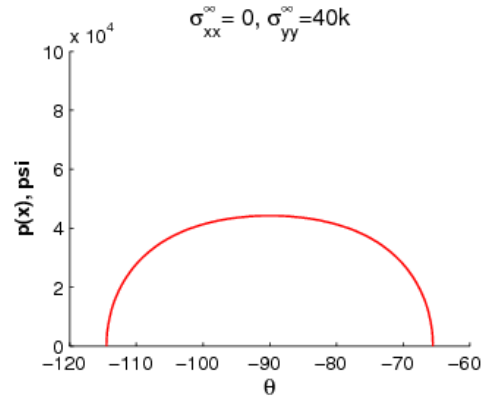
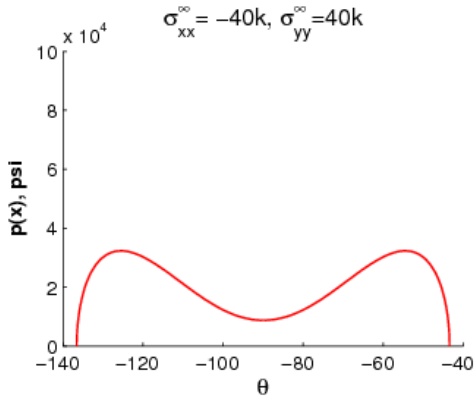
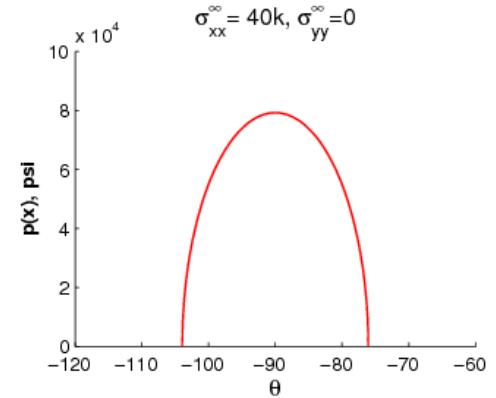
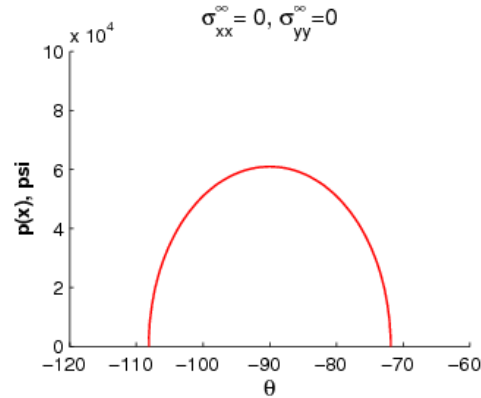
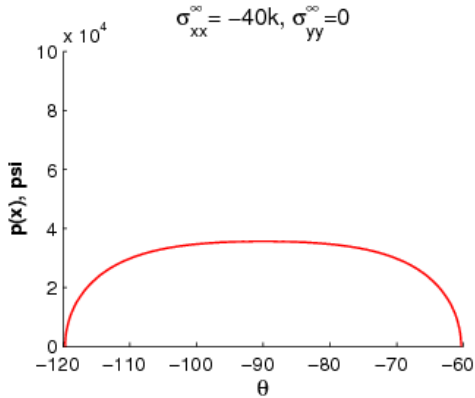
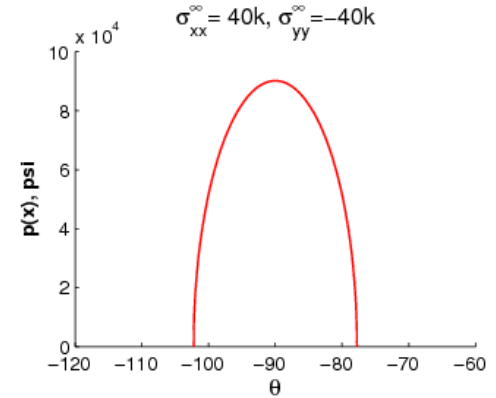
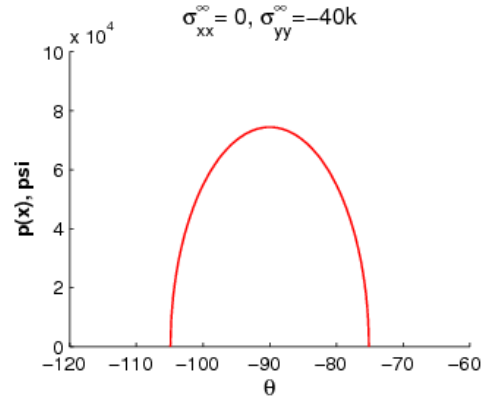
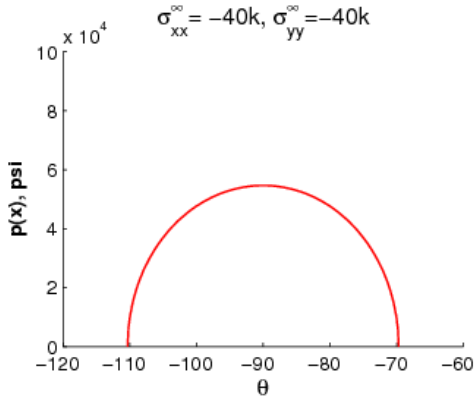
# PIN LOAD ONLY

- Conformal contacts  $\mu = 0$
- $R = 1.0''$   $R_d = 0.99''$
- $E = 1.708 \times 10^7$   $\nu = 0.316$
- Plane strain,  $\kappa = 1.735$
- $P = 10k, 20k, 40k$
- Solution of Singular Integro-Differential Equation using modified Gauss-Chebyshev method
- Solid line (SIDE), Marker (FEM)





# REMOTE STRESSES + PIN LOAD



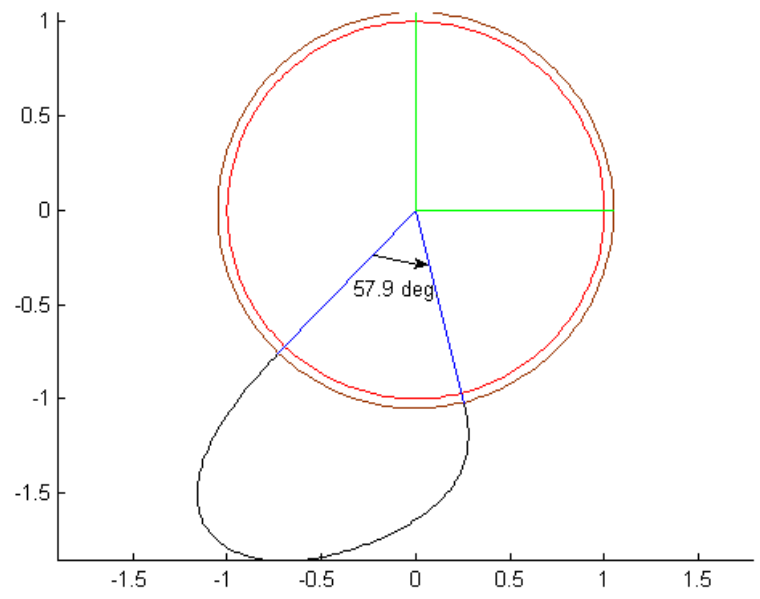
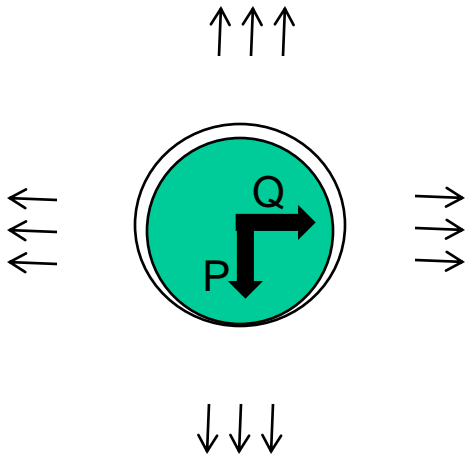
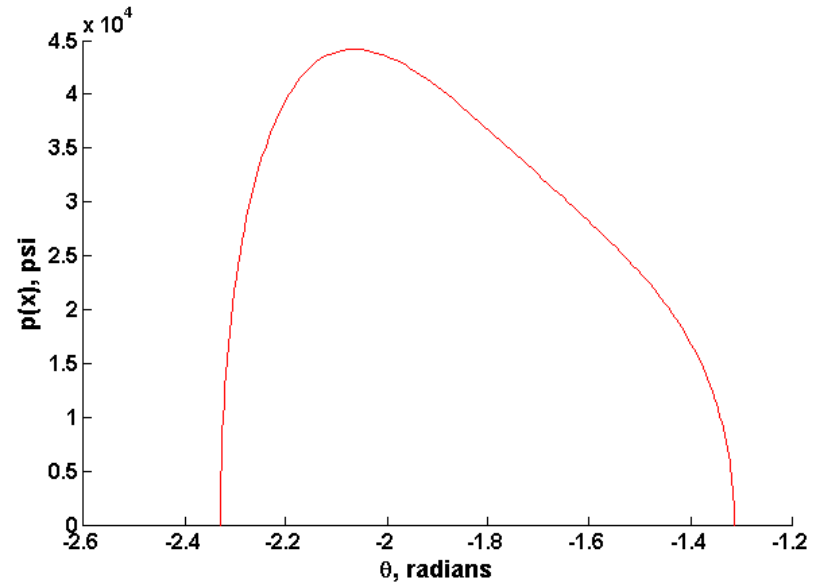
$R = 1.0''$   
 $Rd = 0.98''$   
 $\kappa = 1.735$   
 $P = 30k$   
 (all cases)

$\sigma_{xx} =$   
 $-40, 0, 40$  ksi  
 $\sigma_{yy} =$   
 $-40, 0, 40$  ksi



# Oblique pin load+remote stresses

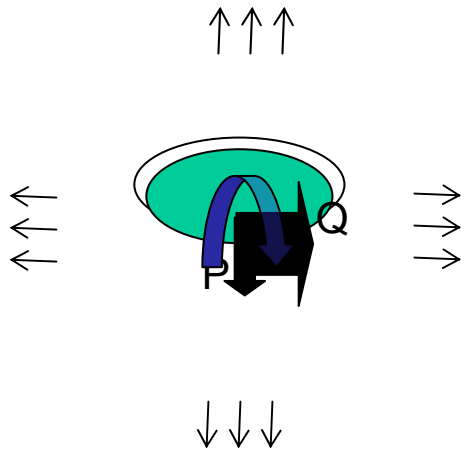
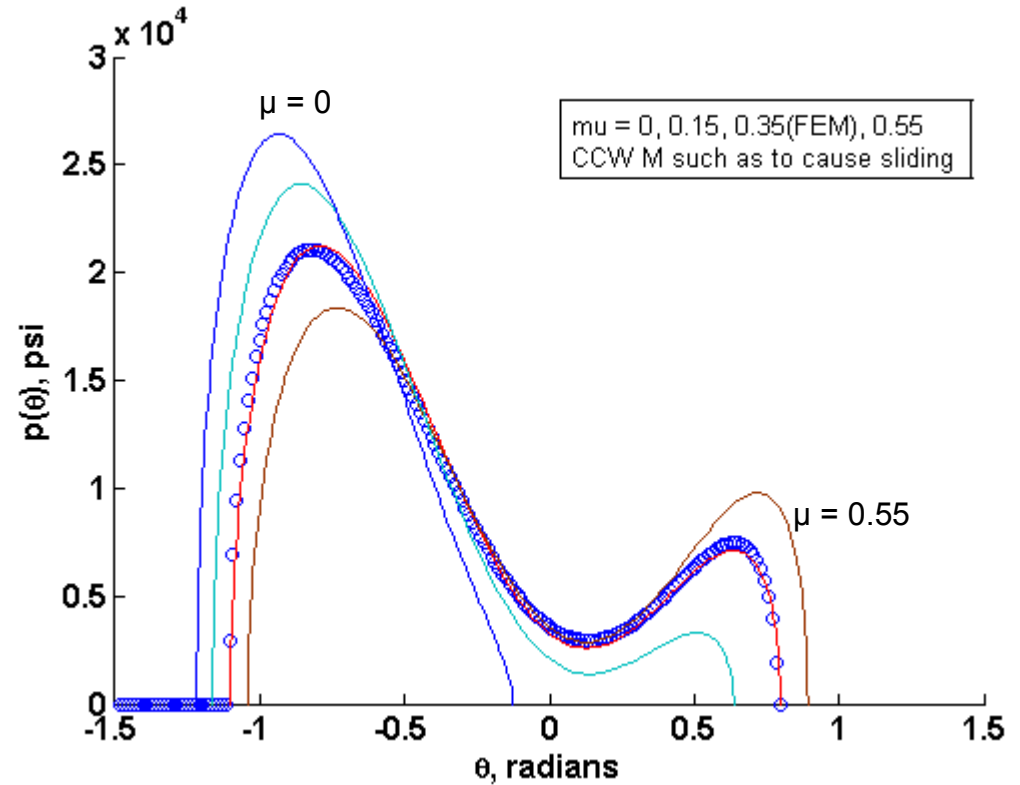
- Equivalent to P only + additional  $\sigma_{xy}$  at infinity when  $\mu = 0$
- Essential to include Q in formulation because in presence of friction this is not possible without loss of generality
- $\kappa = 1.735$   $R=1''$ ,  $Rd=0.98''$ ,  $P=30k$ ,  $Q=-10k$   $\sigma_{xx} = -10ksi$ ,  $\sigma_{yy} = 50 ksi$





# Generalized case of bulk-sliding

- $\mu = 0.0, 0.15, 0.35, 0.55$
- $R = 1.0''$   $R_d = 0.995''$
- $E = 17.08 \times 10^6$   $\nu = 0.316$
- Plane strain,  $\kappa = 1.735$
- $P = 12.5k$ ,  $Q = 12.5k$
- $\sigma_{xx} = -12$  ksi,  $\sigma_{yy} = 12$  ksi
- Solid lines (SIDE), Marker (FEM, very near sliding)

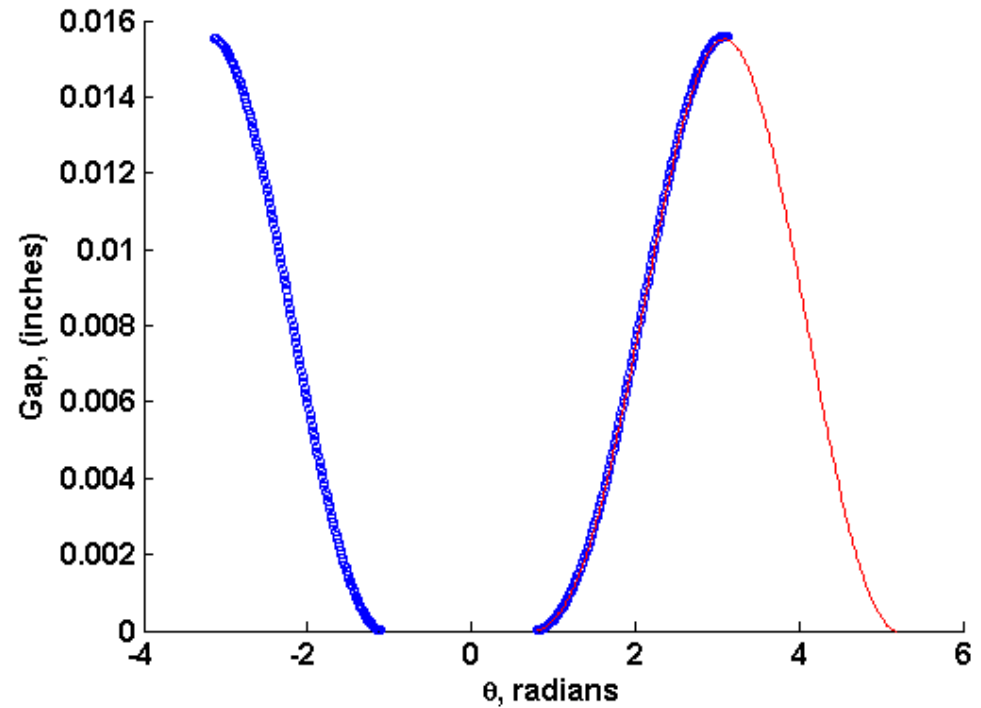




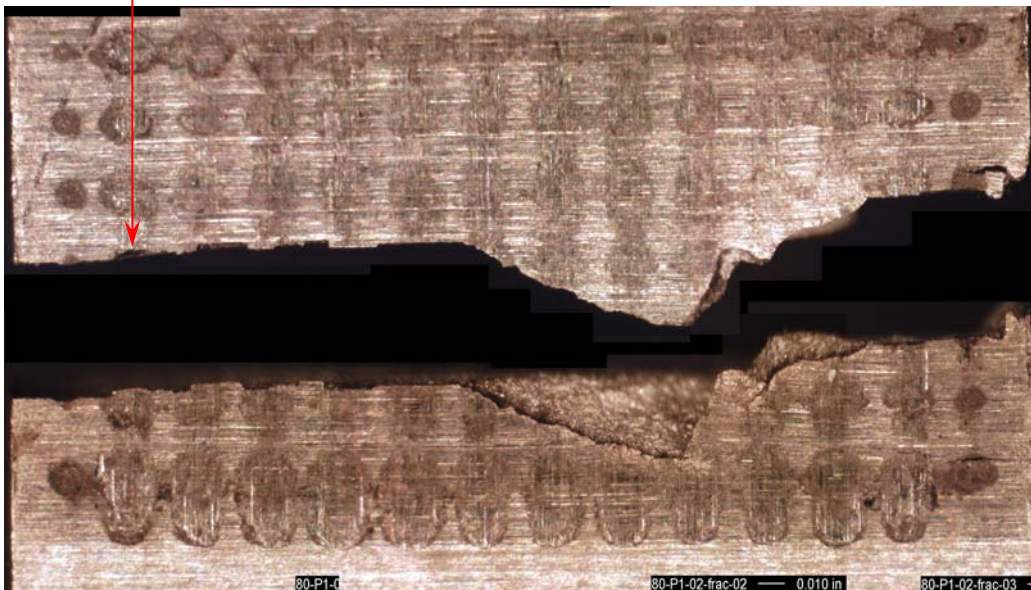
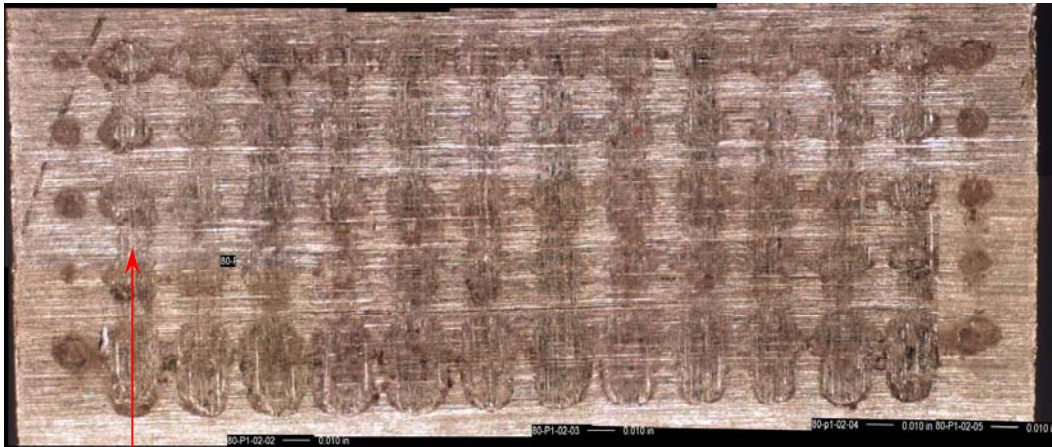


# Results: Gap and approach for a full sliding problem

- Problem same as discussed before: has P,Q, stresses
- $\mu = 0.35$
- Solid line SIDE + 2pt. bvp gap
- Markers FEM
- Points separated by  $2\pi$  are identical
- SIDE predicted sliding moment  $M_{cr} = -6608$ , FEM  $\sim -6635$
- **Previous results due to Persson and Ciavarella and Decuzzi**



# LSP Contact Surface



- Top picture is prior to testing
- Bottom picture indicates fracture along middle of contact
- Arrow indicates origin of fatigue crack